LECTURE PLAN

Course Name:Engineering MathematicsCourse code:MA1201Academic Year:2016 – 17Class:BEAcademic Session:Monsoon 2017Semester:IPre-requisite(s):Basics of Algebra, Calculus, Trigonometry, Coordinate Geometry

Credits: 4 (3 Lectures, 1 Tutorial)

<u>Course Description:</u> This course is intended as a basic course which enables the students to get the detailed idea about: infinite sequences and series, functions of two or more variables, their differentiation, properties and applications, integral calculus - multiple integrals and their applications, polar equations of conics and their properties, vector differential calculus, and vector integral calculus.

<u>Course Outcomes</u>: After completion of the course, the learners will be able to: decide the behaviour of sequences and series using appropriate tests, get an understanding of partial derivatives and their applications in finding maxima - minima problems, apply the principles of integral to solve a variety of practical problems in engineering and sciences, gain an understanding of polar equations of conics, their tangent, normal, chord of contact etc., solve problems involving derivatives (gradient, divergence, curl etc.) and integrals (surface, volume etc.) of vector functions, demonstrate a depth of understanding in advanced mathematical topics, and enhance and develop the ability of using the language of mathematics in engineering.

Course Coordinator: Dr. (Mrs.) Anjana Pradhan Ghorai

Team of Faculty members: Dr. (Ms.) Prabjot Kaur, Dr. AbhinavTandon, Dr. SatyabrataAdhikari,

Dr.Randhir Singh, Dr.(Ms.) S. D. Jabeen.

Text Books:

TB 1: M.D. Weir, J. Hass and F. R. Giordano: Thomas' Calculus, 11th edition, Pearson Educations, 2008. **TB** 2: Dennis G. Zill and Warren S. Wright: Advanced Engineering Mathematics, 4th edition, Jones andBartlertt Publishers, 2010

Reference Books:

RB 1: E. Kreyszig: Advanced Engineering Mathematics, 8th Edition John Wiley and sons 1999.

RB 2: T.M. Apostol: Calculus Vols 1 and 11.2ndEdition(reprint), John Wiley and sons, 2015.

RB 3: Robert Wrede& Murray R. Spiegel, Advanced Calculus, 3rd Ed., Schaum's outline series, McGraw-Hill Companies, Inc.,2010.

| Serial No. | Learning objectives | Topic(s) to be covered | Lecture Hr. | Preferred Book(s) | Total no. of Lecture Hrs. |
|---------------|---|--|----------------|----------------------|------------------------------------|
| Module I | The aim of these lectures is to introduce the concept of a sequence which arises naturally in various fields. | Sequences, bounded sequences, upper and lower bounds, monotonic sequences | 1 | TB1 | 3 |
| | | limits of a sequence, convergence of sequence | 2 | TB1 | |
| | | Cauchy's general principle of convergence, Cauchy's theorems on limits (No proof). | 3 | RB3 | |
| Module II | The aim of these lectures is to gain knowledge of how to add | Convergence of series of real numbers of | 4-5 | TB1 | 7 |

| | infinitely many numbers | positive terms, p - series | | | |
|--------|---|--|--------------|------|---|
| | together. which leads to the theory of infinite series. | test Cauchy's root test, D' | 6-8 | TB1 | |
| | This theory is applicable to deal | Alembert's ratio test, | 0-0 | & | |
| | with general functions which | Raabe's test. Gauss's | | RB3 | |
| | are often solutions to important | Ratio Test, Logarithmic | | RBS | |
| | problems in science and | and Higher logarithmic | | | |
| | engineering. | Ratio | | | |
| | | Leibnitz's Rule for alternating series Test. | 9 | TB1 | |
| | | Absolute and | 10 | TB1 | |
| | | conditional convergence | 10 | 111 | |
| Module | The aim of these lectures is to | Generalized Mean | 11 | TB1 | 9 |
| III | deal with the representation of | Value Theorem, | | 121 | |
| | the known differentiable | Maclaurin's series, | | | |
| | function as an infinite sum of | Taylor's series of | | | |
| | power of x. | functions | | | |
| | As most entities in the real | Functions of several | 12-13 | TB1 | |
| | world are dependent of several | variables, level curves, | | | |
| | independent entities, the | limits, continuity, | | | |
| | Functions of several variables, | partial Derivatives. | | | |
| | its limits, continuity and | Euler's theorem on | 14 | RB3 | |
| | differentiability has been introduced. | Homogeneous functions | 15 16 | TD 1 | |
| | miroduced. | Chain Rule, transformation of | 15-16 | TB1 | |
| | | transformation of independent variables, | | | |
| | | total differential, | | | |
| | | Jacobians. | | | |
| | | Taylor's series in two or | 17 | TB1 | |
| | | more variables. | | | |
| | | Maximum, minimum | 18-19 | TB1 | |
| | | and saddle points of | | | |
| | | functions of two | | | |
| | | variables. Several | | | |
| | | independent variables | | | |
| | | Lagrange's method of | | | |
| | | Undetermined Multipliers. | | | |
| Module | These lectures introduce the | Beta and Gamma | 20 | RB1 | 6 |
| IV | integrals of functions of several | functions. | 20 | KDI | |
| | variables over a region in plane | Double integrals, area, | 21-22 | TB1 | 1 |
| | and space. The theory of | | | | |
| | multiple integrals has wide | integration, evaluation | | | |
| | range of application specially in | of integrals by | | | |
| | calculating volumes, areas in | transforming into polar | | | |
| | plane, moments and centers of | co-ordinates. | | TD 1 | 4 |
| | mass etc. | Evaluation of Triple | 23 | TB1 | |
| | | integrals. Volume and surface | 24-25 | TB1 | 1 |
| | | area by double and | 44-43 | IDI | |
| | | area by double alla | | | |

| Module V | Polar coordinates are especially important in Astronomy and Astronautical engineering because the satellites, moons, planets all move with respect to a point(sun) and approximately move along the ellipses, parabolas, hyperbolas etc. All these curves can be described with a single relatively simple polar equation. | triple integration by transforming in to cylindrical and spherical polar coordinates Sketching polar equations of conic section. Equation of chord, tangent and normal line to a conic section. equation of chord of contact, director circle and asymptote to a conic section. | 26 27 28-29 | TB1 | 4 |
|---------------|--|--|-------------------|------------|---|
| Module VI | | First order differential equations, linear and Bernoulli's equation, Reduction of order. | 30 | TB2 | 7 |
| | In these lectures, the calculus of vector valued functions are | Curvature, normal vector, torsion and TNB | 31 | TB1 | |
| | introduced to describe the paths and motions of objects moving | frame Tangential and normal | 32-33 | TB2 TB1 | |
| | in a plane or space. The new quantities that describe how an object's path can turn and twist in space are also introduced. | components of velocity and acceleration, radial and transverse acceleration, Motion in polar and cylindrical coordinates | 32-33 | & TB2 | |
| | | Directional derivative, Gradient, Divergence and curl. Expansions, identities. Tangent plane and normal line. | 34-35 | TB2 | |
| | | Gradient, divergence and curl in curvilinear coordinates. | 36 | TB2 | |
| Module VII | In these lectures, the theory of integration is extended to curves and surfaces in a plane or space. The fundamental theorem of vector integral calculus and its | Line integrals, Work, Circulation, Flux, Path independence, Potential function, Conservative field, | 37-38 | TB2 | 4 |
| | mathematical consequence is discussed along with physical applications. | Green's theorem in plane, surface and volume integrals Gauss's Divergence theorem, Stoke's theorem. Applications | 39-40 | TB2 | |

Assessment tools & Evaluation procedure

| Assessment Tool | % Contribution during Assessment |
|---------------------------------|----------------------------------|
| Mid Sem. Examination Marks | 25 |
| End Sem. Examination Marks | 60 |
| Quiz (Best of Two out of Three) | 15 |

NOTICE: All notices related to the course will be displayed in the Department of Mathematics notice board.